



# Mobility Data Management & Exploration

Ch. 03.  
Modeling and Acquiring  
Mobility Data

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*“It is a very sad thing that nowadays there is so little useless information.” Oscar Wilde*

# Chapter outline

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## 3.1. Modeling Mobility Data

## 3.2. Acquiring Trajectories from Raw Data

## 3.3. Trajectory Reconstruction and Simplification

## 3.4. Trajectory Data Generators

## 3.5. Summary

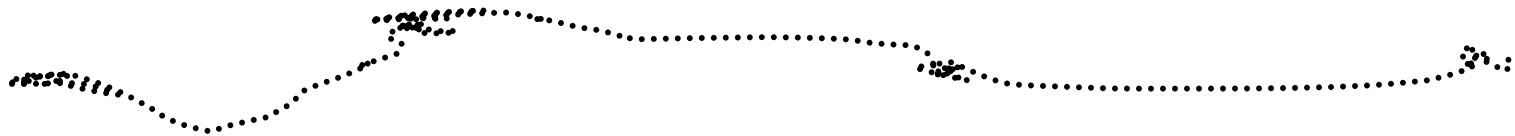


## 3.1.

### Modeling mobility data

# Trajectory definition

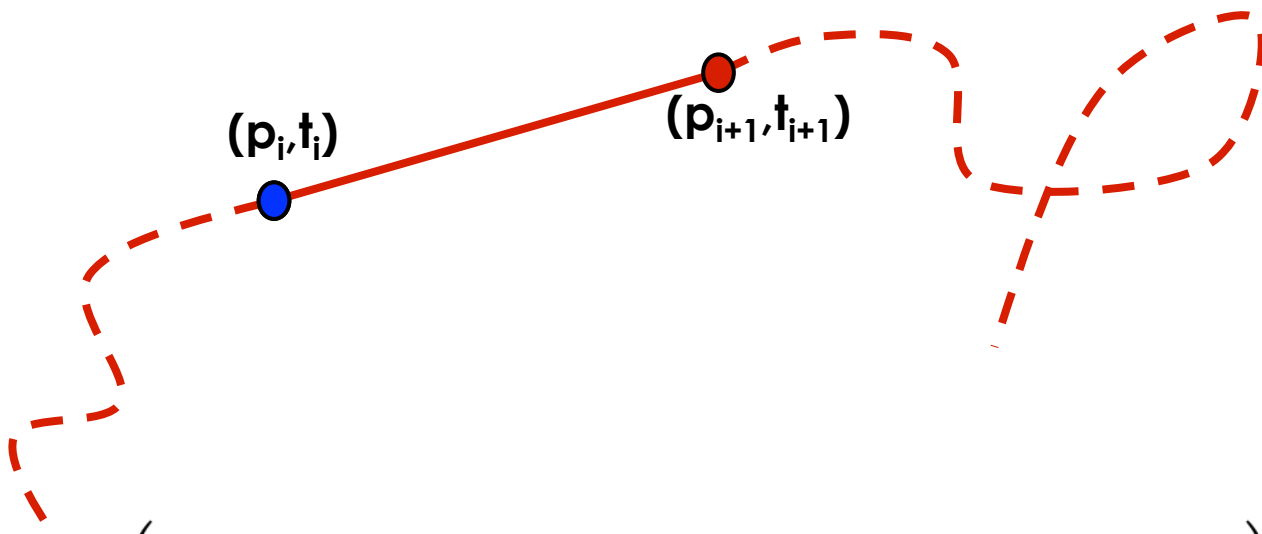
- A **trajectory** is a model for a motion path of a moving object (human, animal, robot, ...)
- (due to discretization) a sequence of sampled time-stamped locations  $(p_i, t_i)$  where  $p_i$  is a 2D point  $(x_i, y_i)$  and  $t_i$  is the recording timestamp of  $p_i$



$$T = \{ \langle p_1, t_1 \rangle, \langle p_2, t_2 \rangle, \dots, \langle p_n, t_n \rangle \}$$

# Trajectory definition (cont.)

- A common representation of a trajectory is a **3D polyline** whose vertices correspond to time-stamped locations  $(p_i, t_i)$ 
  - Usually, **linear interpolation** is assumed between  $(p_i, t_i)$  and  $(p_{i+1}, t_{i+1})$

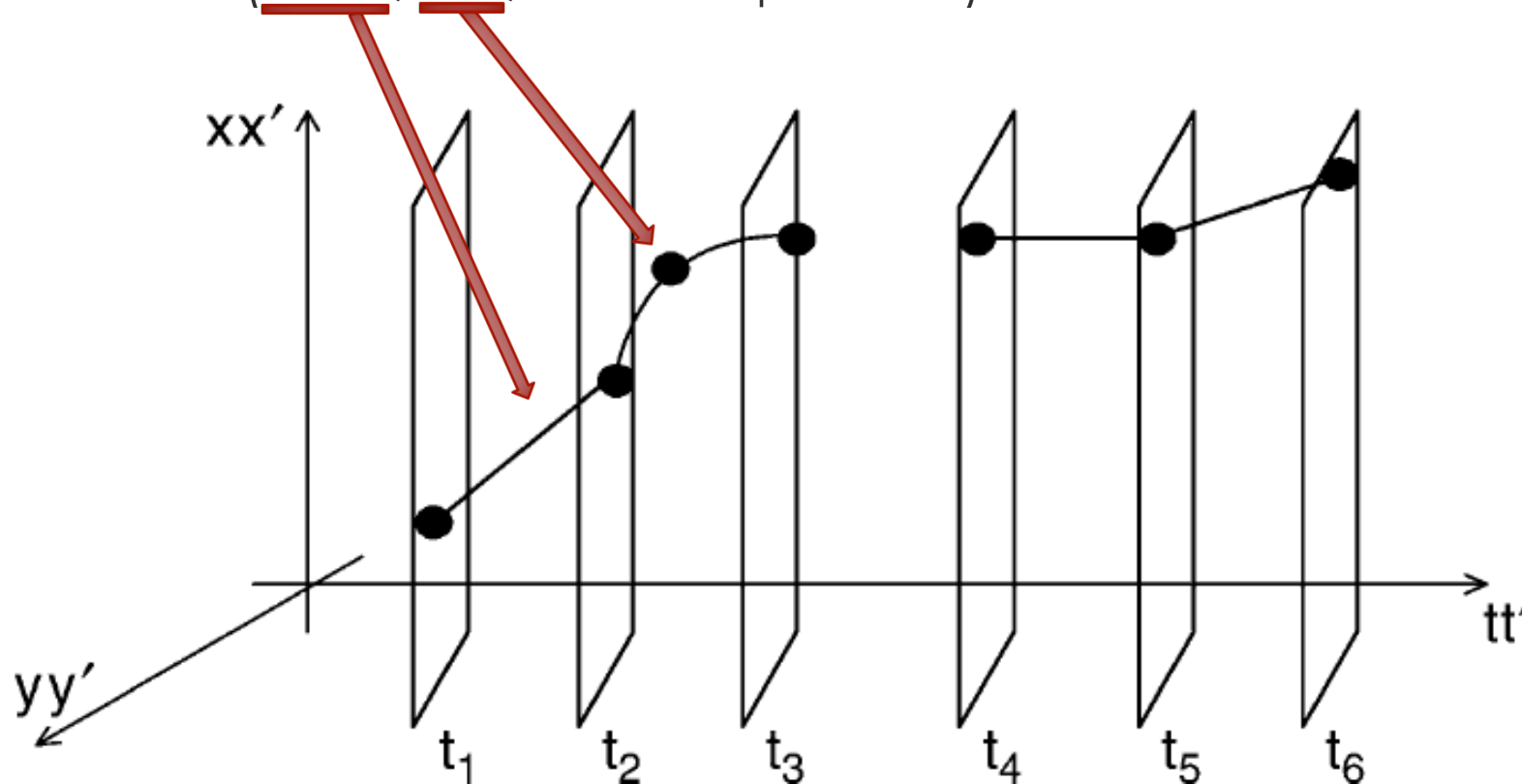


The diagram illustrates a segment of a trajectory. A solid red line connects two points: a blue dot labeled  $(p_i, t_i)$  and a red dot labeled  $(p_{i+1}, t_{i+1})$ . This solid line represents linear interpolation. Dashed red lines extend from these points to show the overall path, which includes a loop. The equation below defines the position  $p(t)$  at any time  $t$  between  $t_i$  and  $t_{i+1}$ .

$$p(t) = \left( x_i + \frac{t - t_i}{t_{i+1} - t_i} (x_{i+1} - x_i), y_i + \frac{t - t_i}{t_{i+1} - t_i} (y_{i+1} - y_i) \right)$$

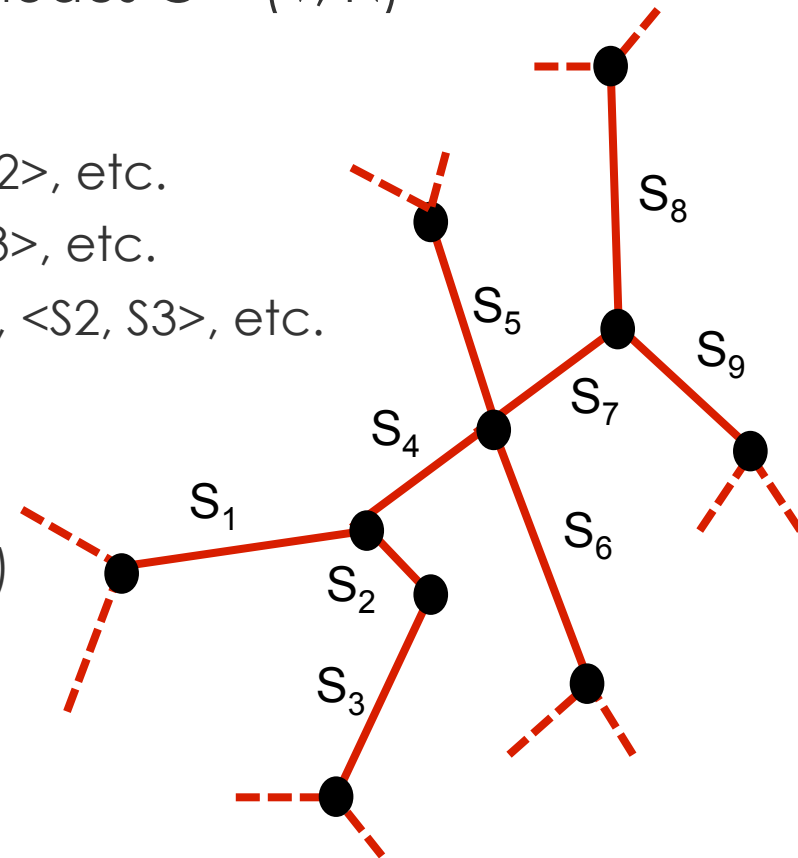
# Sliced representation

- Decomposes the temporal development into '**slices**'
- Within each slice, the movement is modeled by a 'simple' function (linear, arc, etc. interpolation)



# Movement on a network

- Network-constrained movement assumes an underlying network / graph of vertices and nodes  $G = (V, N)$
- Alternative models:
  - **Segment-oriented model**:  $\langle S1 \rangle$ ,  $\langle S2 \rangle$ , etc.
  - **Edge-oriented model**:  $\langle S1 \rangle$ ,  $\langle S2, S3 \rangle$ , etc.
  - **Route-oriented model**:  $\langle S1, S4, S7 \rangle$ ,  $\langle S2, S3 \rangle$ , etc.
- The location of an object is represented by:
  - the entity (segment / edge / route) it is located on and
  - an offset in  $[0, 1]$  denoting the relative location in the entity





## 3.2.

Acquiring trajectories  
from raw data

# Raw Data

- Example of GPS recordings

<trk>

...

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<time>2013-01-19T08:54:57.608Z</time> </trkpt>

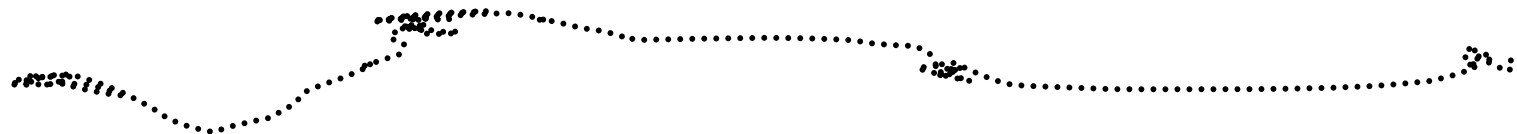
<trkpt lat="38.17725880" lon="23.74043843"> <ele>1117.98</ele>  
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...

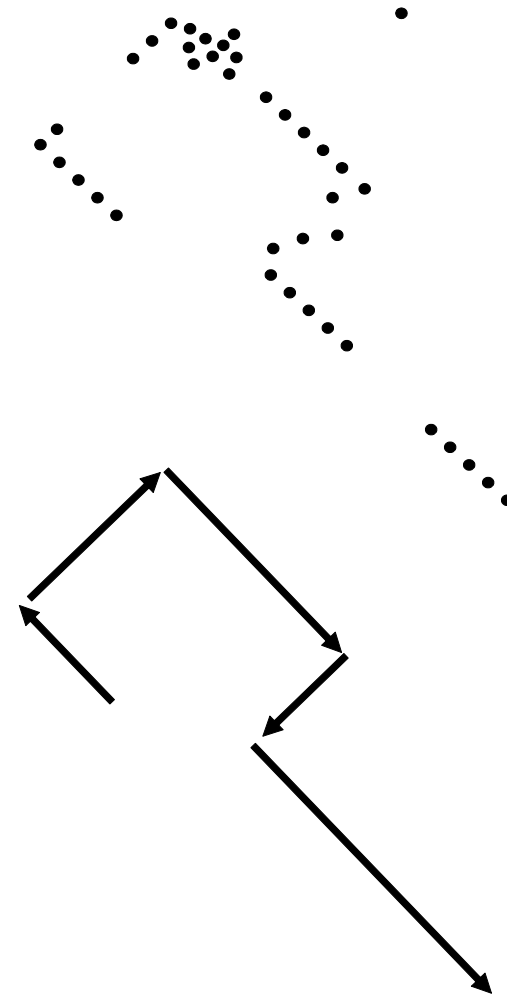
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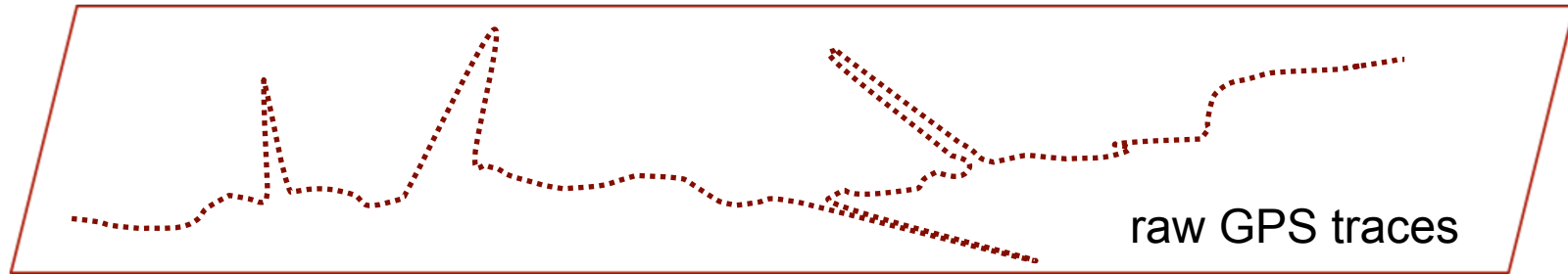
# Acquiring Trajectories from Raw Data

The problem:

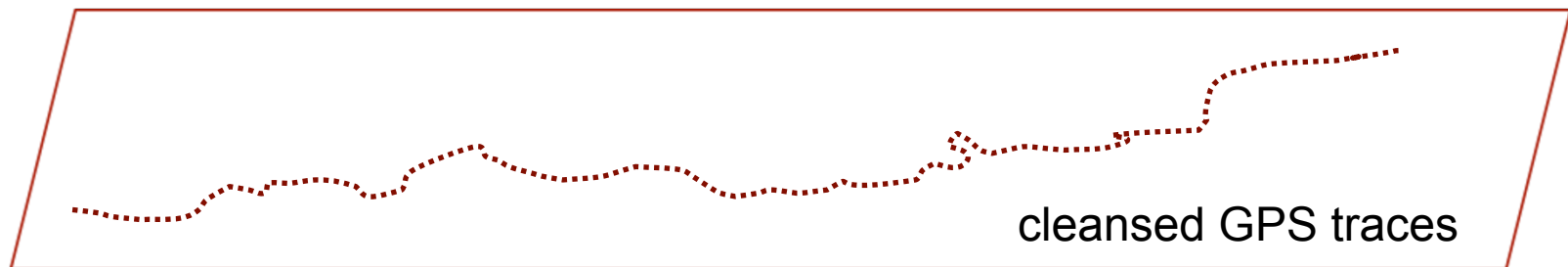
- **From raw data**, i.e., successive time-stamped locations ...
- ... **to meaningful trajectories**, i.e., continuous development of movement



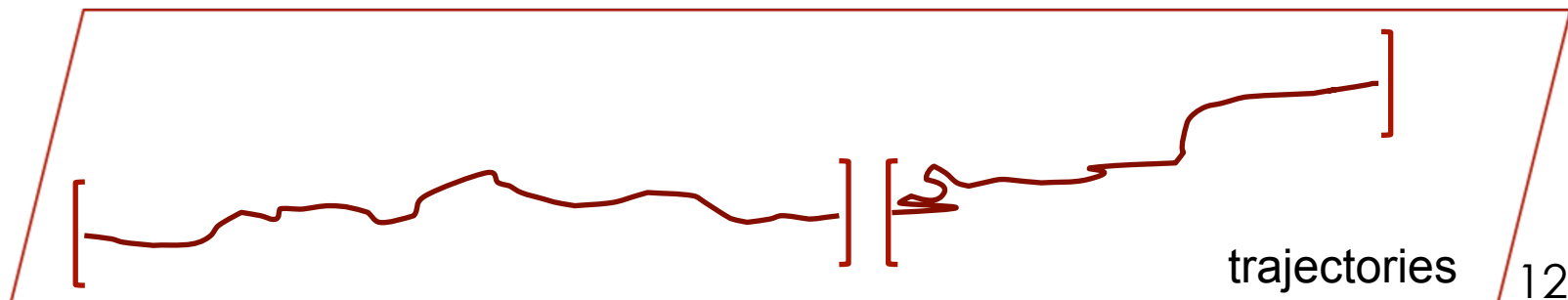
# A two-step methodology



- Step 1: **data cleansing**

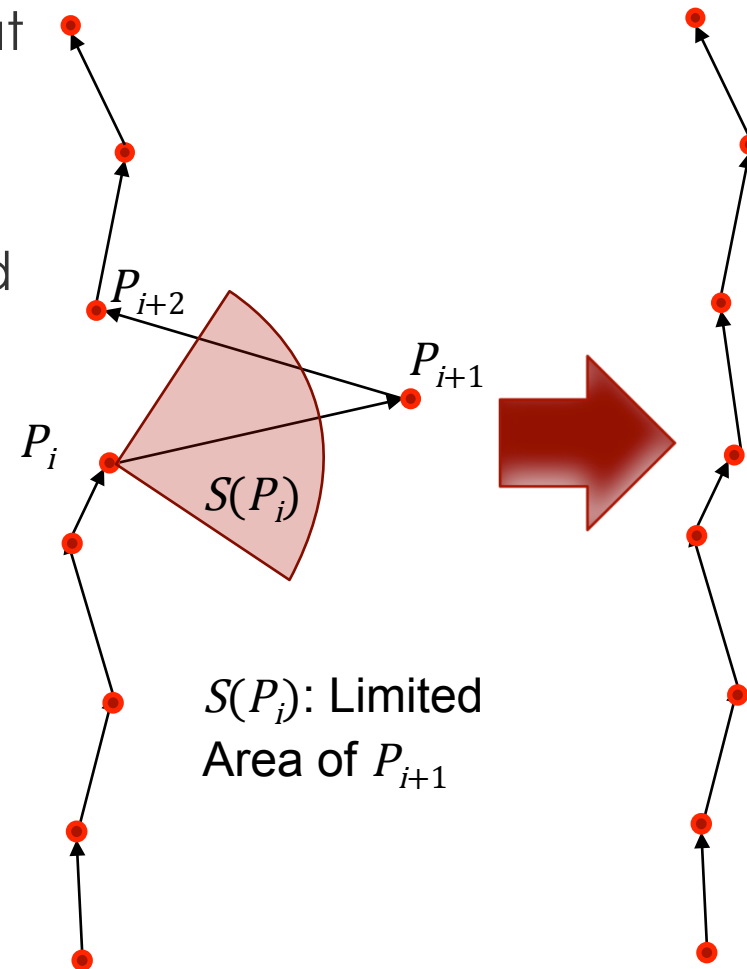


- Step 2: **trajectory identification**



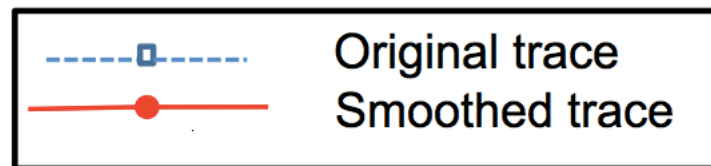
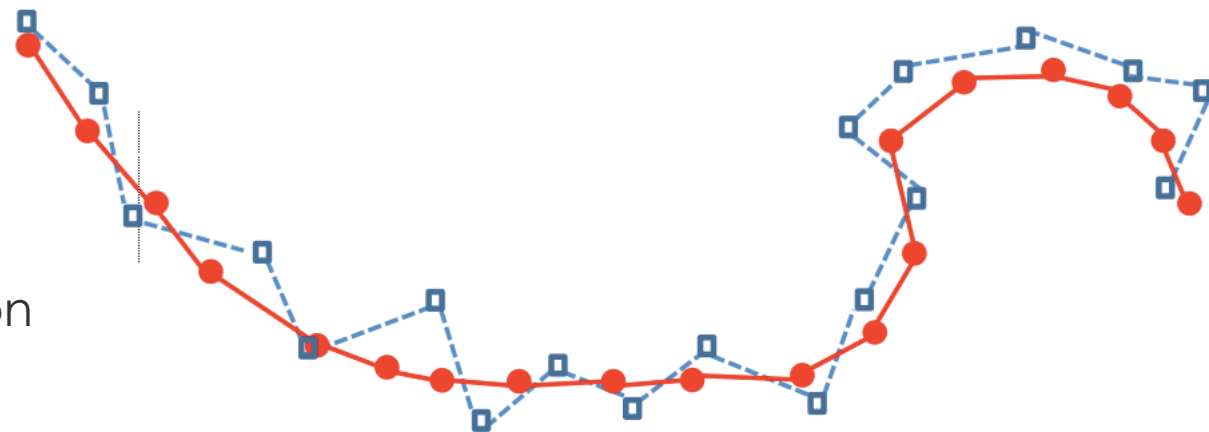
# GPS Data Cleansing

- Erroneous recordings: noise vs. random errors
- **Noise** corresponds to values that are 'impossible' to appear
- Can be detected and removed using appropriate filters
  - e.g. maximum speed



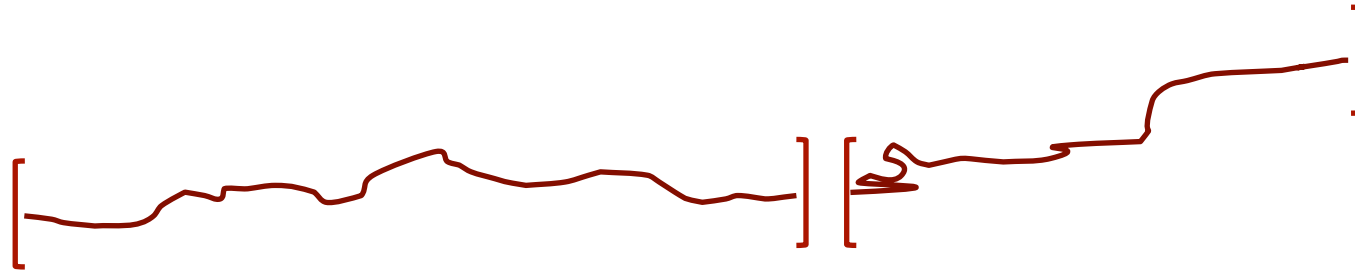
# GPS Data Cleansing (cont.)

- Erroneous recordings: noise vs. random errors
- **Random errors** correspond to 'possible' values that appear to be small deviations from actual ones
- Can be smoothed using statistical methods
  - e.g. least squares  
spline approximation



# Trajectory identification

- Goal 1: **Interpolate successive points** in order to simulate the continuous nature of movement
  - Linear interpolation (the most popular), Bezier curves, etc.



- Goal 2: **Segment sequences of points** in homogeneous sub-sequences (= trajectories)
  - Identification via raw (spatial / temporal) gap
  - Identification via prior knowledge (e.g. office hours, sleeping hours)
  - Correlation-based identification (ideas from time-series segmentation)

### 3.3.

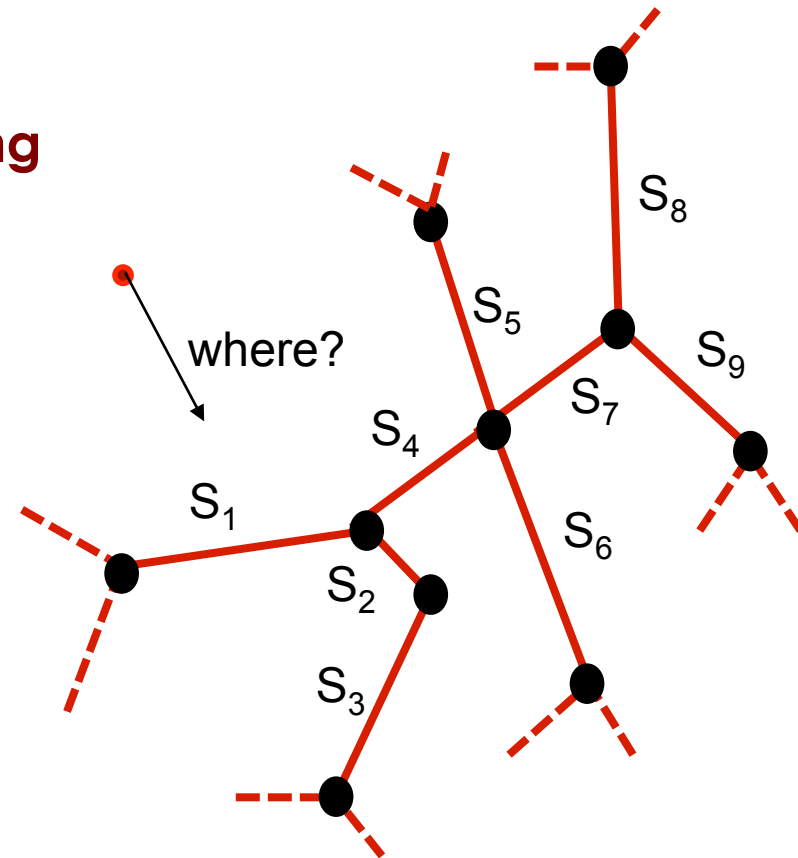
## Trajectory reconstruction and simplification



# Trajectory reconstruction

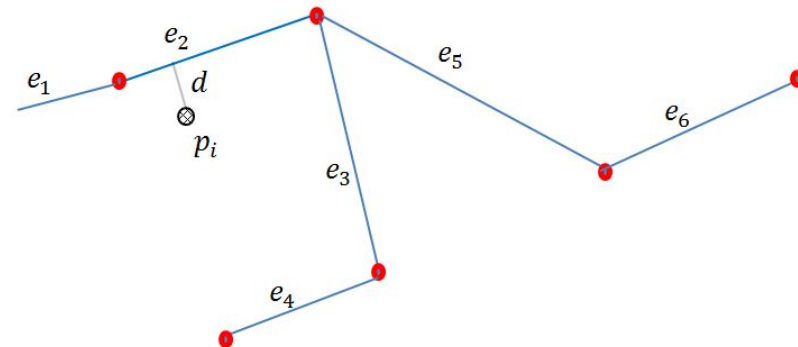
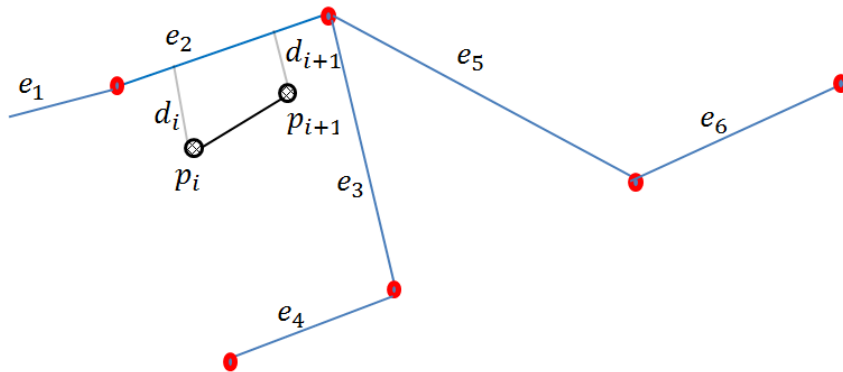
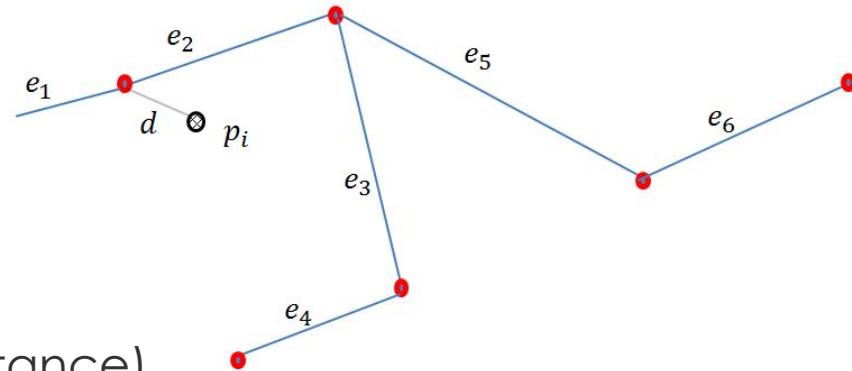
... considering network-constrained movement

- An additional step: **map-matching**
  - Geometric map-matching
  - Topological map-matching
  - Probabilistic map-matching
  - Hybrid map-matching



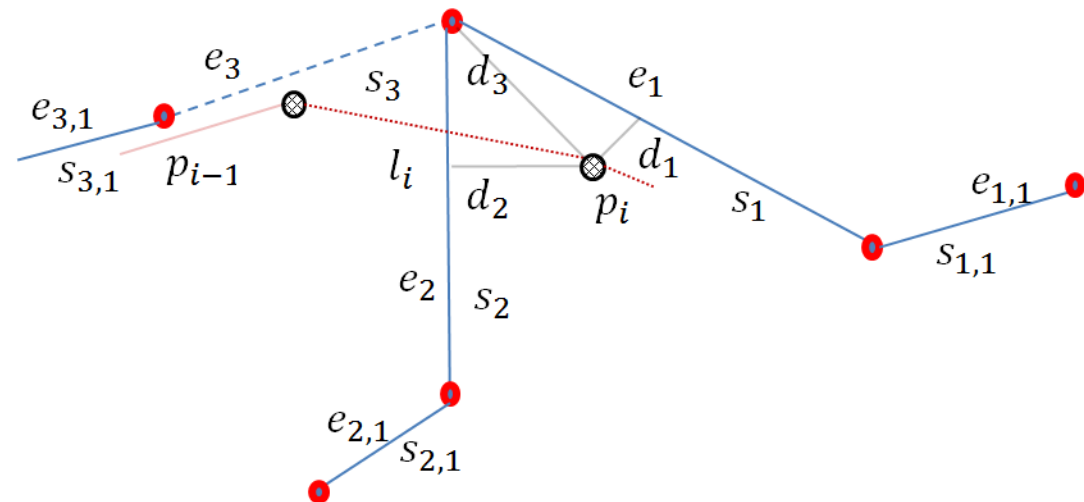
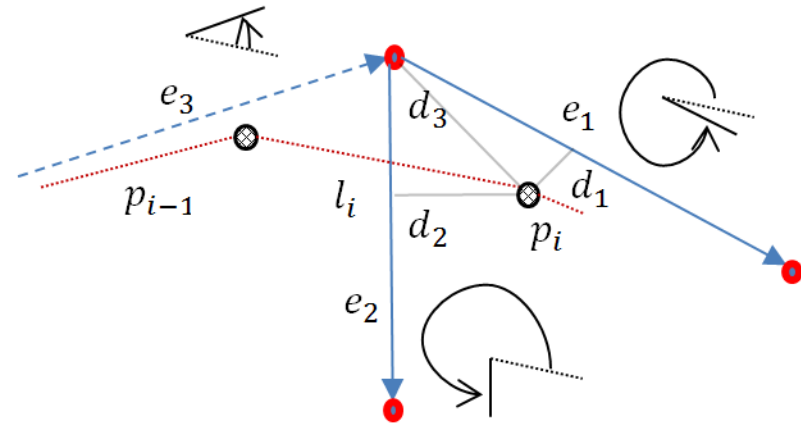
# Geometric map-matching

- The basic idea: map a point into its closest position on the network
- Three types:
  - Point-to-point (e.g. Euclidean distance)
  - Point-to-curve (e.g. perpendicular distance)
  - Curve-to-curve (e.g. Fréchet distance)



# Topological map-matching

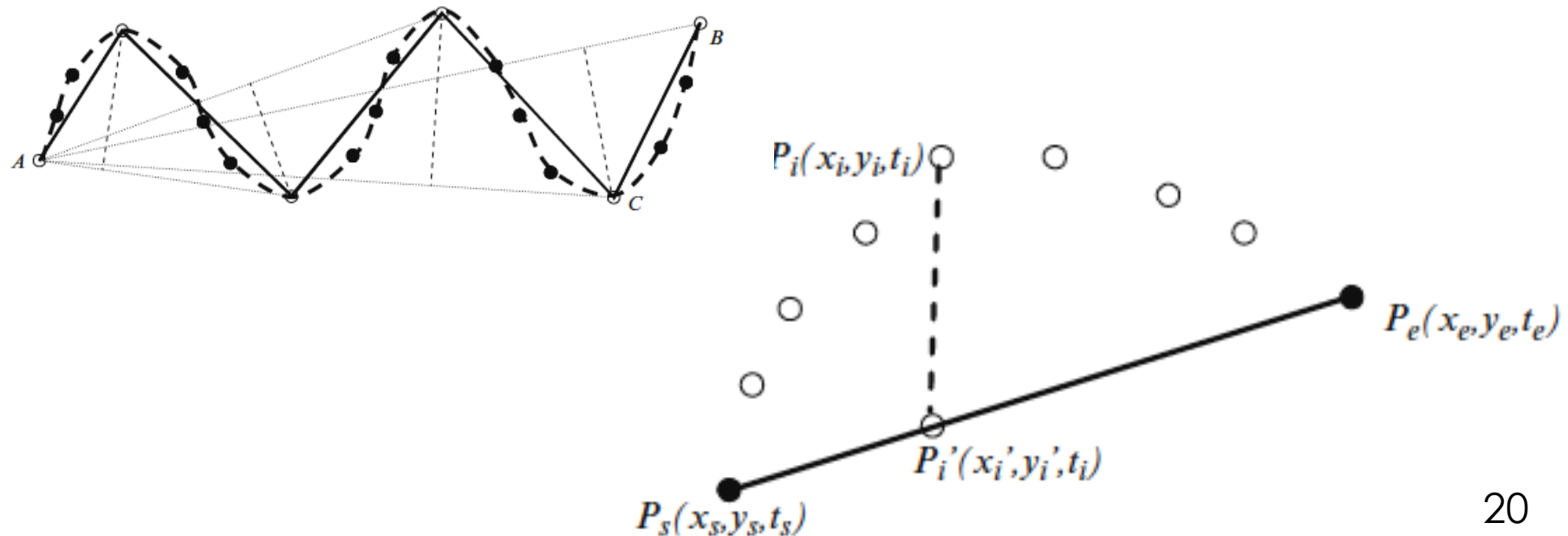
- Utilize both the geometry and the connectivity / adjacency of the graph
- Two steps:
  - Choose the most suitable node(s) of the graph
  - Match the point
- Could be enhanced by a “look-ahead” approach



# Trajectory simplification

... via data compression

- Top-down vs. bottom-up vs. sliding window vs. opening window methods
- From line (e.g. Douglas-Peucker) to trajectory simplification (e.g. Synchronous Euclidean Distance – SED)



## 3.4.

Trajectory data generators

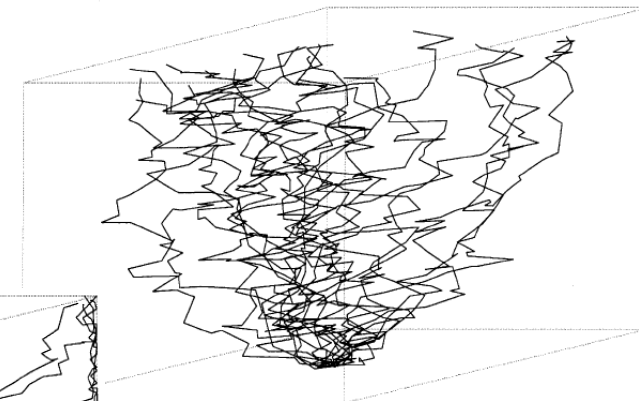
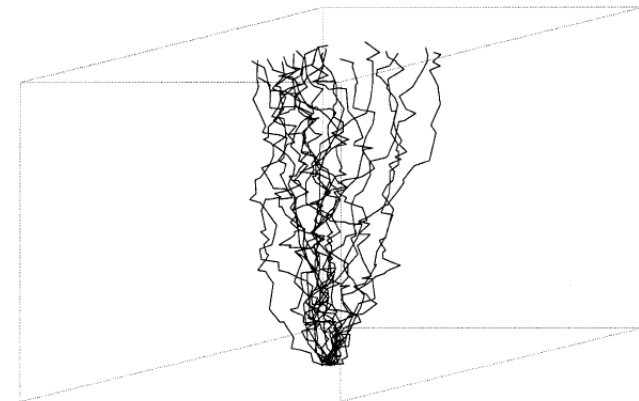
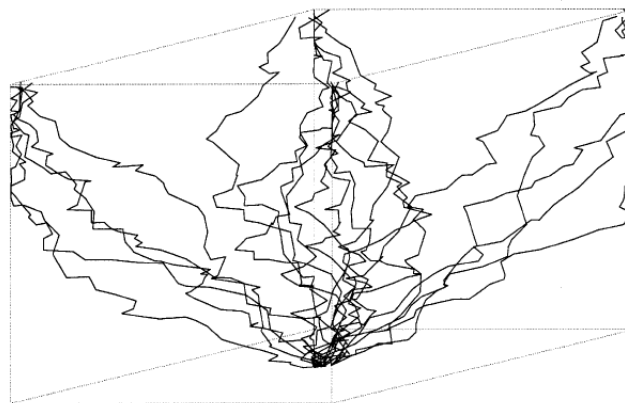
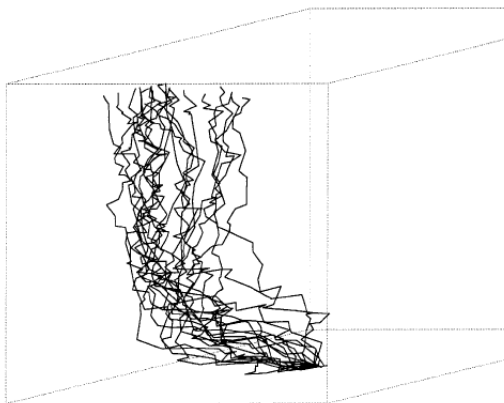
# Why data generators?



- Necessary for performance evaluation purposes
- **Microscopic** (i.e., dealing with single moving objects) vs. **macroscopic** (i.e., dealing with the traffic flow rather than single moving objects)
- Support **free** vs. **network-constrained** movement
  - Examples of generating free movement: **GSTD** (1999), **CENTRE** (2005)
  - Examples of generating network-constrained movement: **Brinkhoff** (2002), **Sumo** (2002), **Gamma** (2005), **BerlinMOD** (2008), **MWGen** (2012), **Hermoupolis** (2013)
  - We present a few next ...

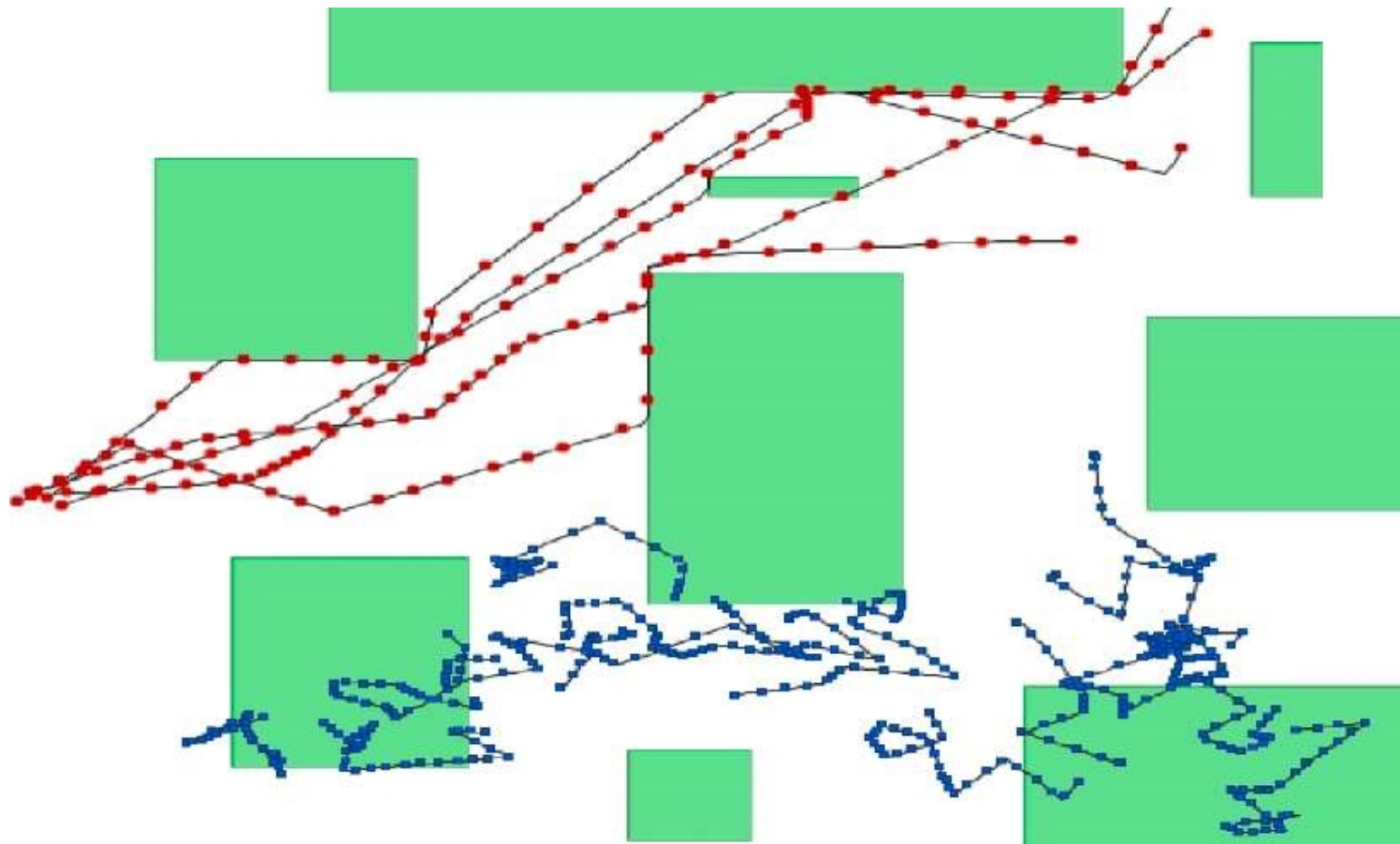
# GSTD (Generating spatio-temporal data)

- Methodology
  - Define starting positions
  - Repeatedly, compute new time-stamped locations
- Thus, simulates different movement behaviors, e.g.
  - slow vs. fast moving objects
  - directed movement towards south vs. the four corners of the horizon



# CENTRE (Cellular Network's Positioning Data Generator)

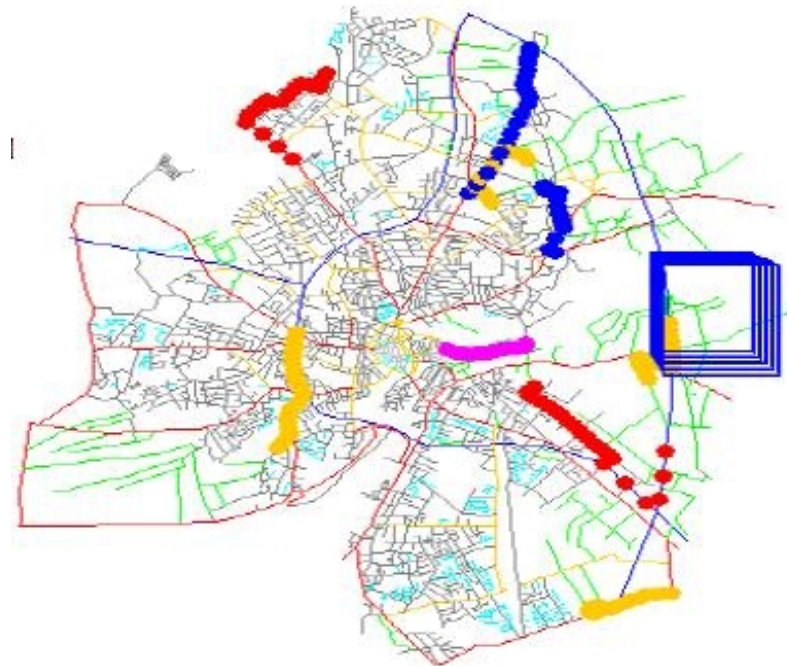
- Simulates groups of objects having different movement behavior and sensitivity to obstacles





# Brinkhoff's generator

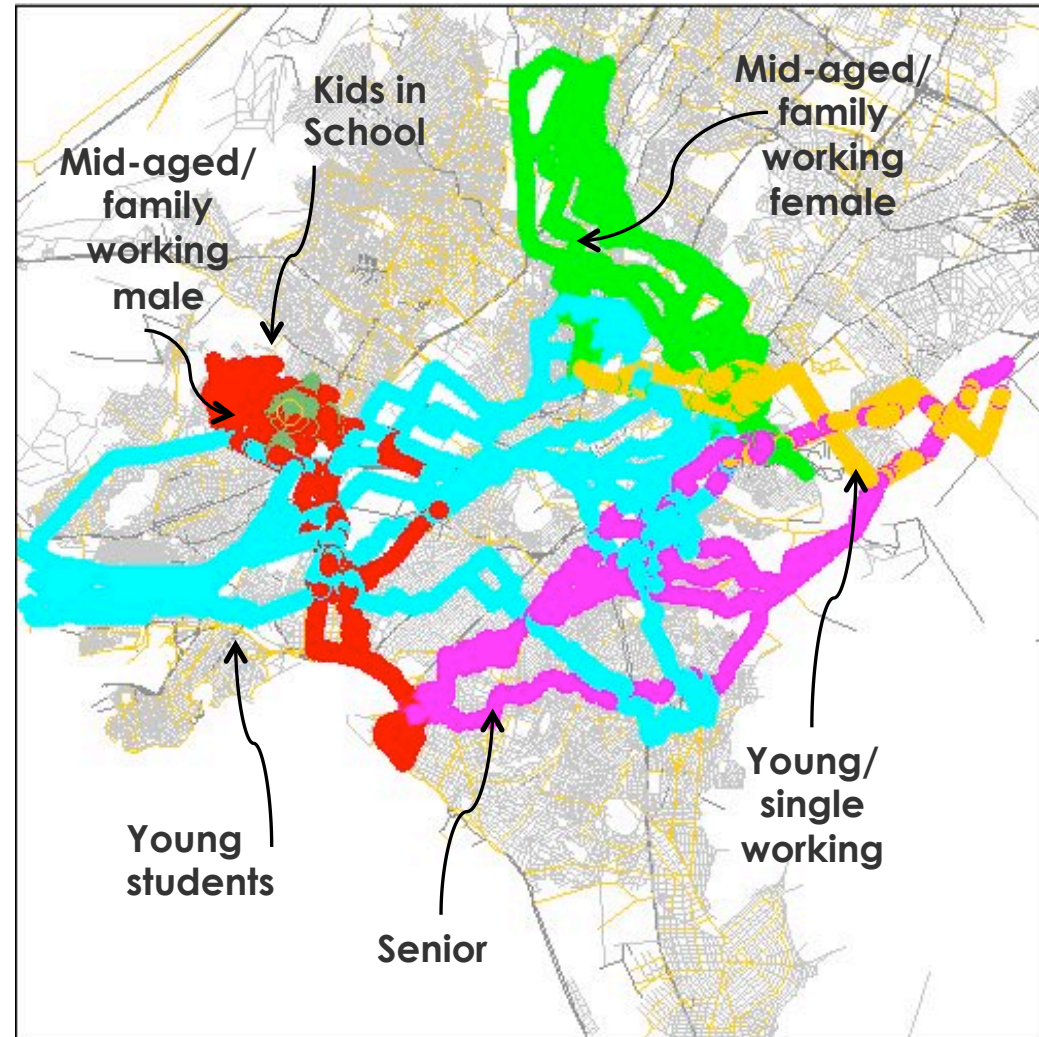
- Methodology:
  - generate starting points
  - generate length of route (depending on object class)
  - generate destination for each object
  - compute the route
  - compute the trajectory by generating a random speed every time unit
    - based on capacity, weather, edge class, etc.



1 : 80000	Time: 0	Delete Obj.	N	obj./begin (M:-100 E:-10):	10	1
				obj./time (M:-40/E:-3):	0	0
Compute	Zoom In	W	E	Zoom Out	Time +	
maximum time (5-400):	20	S	classes (M:1-20/E:1-10):		8	3
report probability (0-1000):	1000	max.speed div. (10=fast,50=middle,250=slow):		50		

# Hermoupolis

- Generate objects moving in an urban area ...
- ... according to different population profiles of given distribution
  - Kids in school: 20%
  - Young students: 10%
  - etc.
- Dual output: synchronized raw (GPS-like) + semantic (annotated) trajectories



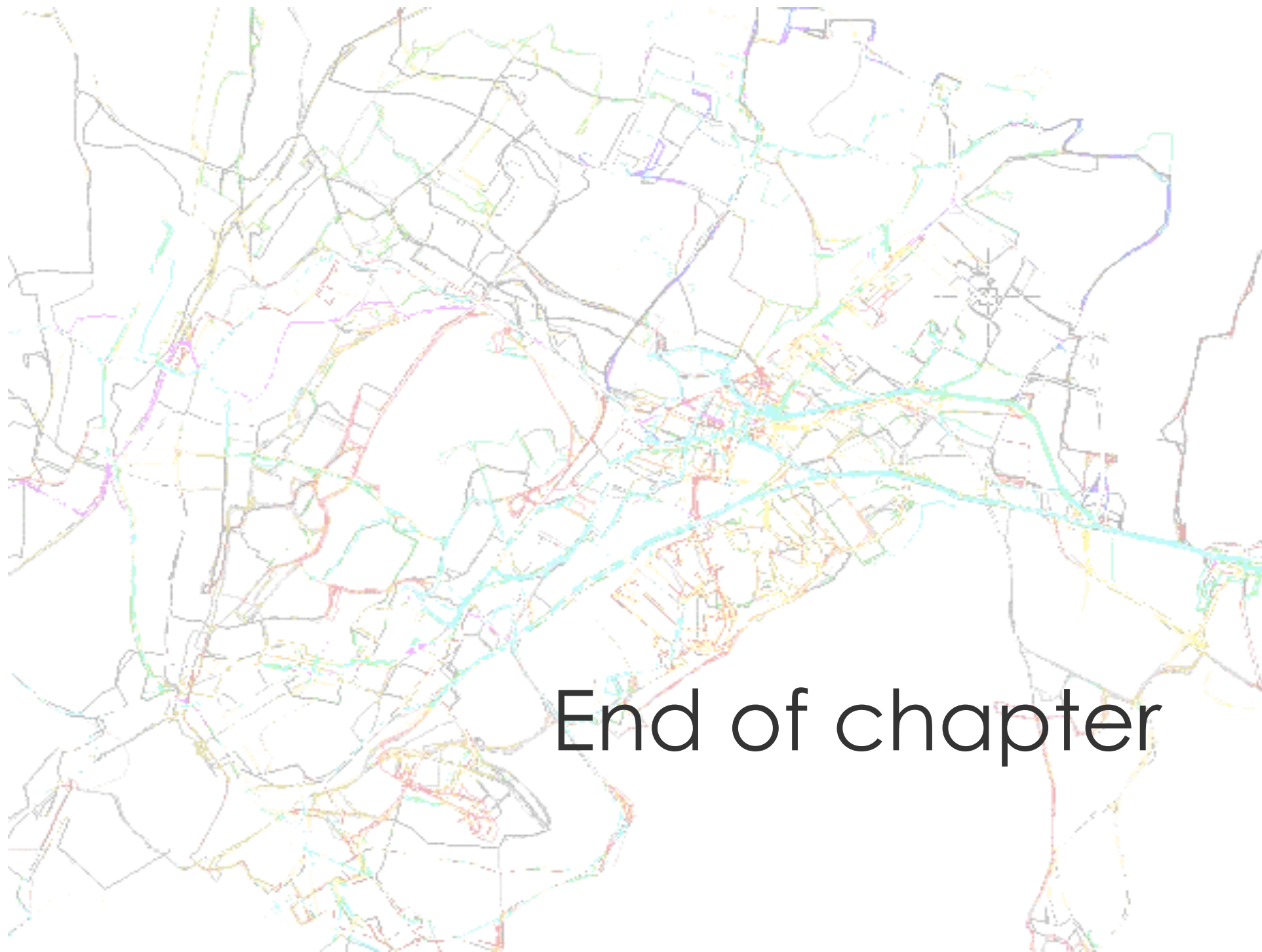
## 3.5. Summary

# Summarizing ...

- In this chapter, we presented the various steps for building meaningful trajectories from raw (GPS-like) data:
  - Data cleansing (noise removal, random errors smoothing)
  - Trajectory identification (point interpolation, trajectory segmentation)
  - Trajectory map-matching
  - Trajectory simplification via data compression
- We also discussed trajectory data generators for evaluation purposes
  - Supporting free vs. network-constrained movement







End of chapter